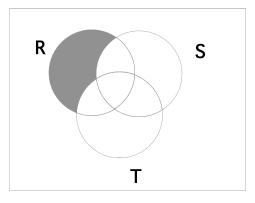
1 Which of the following sets is represented by the shaded region in the Venn diagram below?



 $(a) \quad R \cap T \qquad (b) \quad R \cap (S \cup T) \qquad (c) \quad R \cup (S \cap T) \qquad (d) \quad R \cap (S \cup T)' \qquad (e) \quad R \cup S \cup T$ 

**2** If S and T are sets such that  $n(S \cup T) = 20$ , n(S) = 15,  $n(S \cap T) = 3$ , find n(T).

 $(a) \quad 10 \qquad \qquad (b) \quad 8 \qquad \qquad (c) \quad 15 \qquad \qquad (d) \quad 2 \qquad \qquad (e) \quad 5 \\$ 

**3** Out of 30 job applicants, 11 are female, 17 are college graduates, 7 are bilingual, 3 are female college graduates, 2 are bilingual women, 6 are bilingual college graduates, and 2 are bilingual female college graduates. The number of male college graduates is:

(a) 18 (b) 14 (c) 4 (d) 10 (e) 15

4 On the dinner menu at *The Hogs Breath Cafe*, there is a choice of 5 different appetizers, 10 main courses and 6 desserts. If you wish to order one appetizer, one main course and one dessert, how many different orders could you place?

 $(a) \quad 900 \qquad (b) \quad 21 \qquad (c) \quad 300 \qquad (d) \quad 210 \qquad (e) \quad 400$ 

5 In a round robin Soccer tournament, each team will play each other team exactly once. If there are 10 teams entered in the tournament, how many games must be played?

(a) 13 (b) 55 (c) 120 (d) 17 (e) 45

6 An urn contains 8 pink and 12 blue balls. A sample of size five is drawn from the urn. How many such samples have at least one pink ball.

(a) C(20,5) - C(8,0)C(12,5) (b) C(8,0)C(12,5) (c) C(12,4)C(8,1)

(d) 
$$C(8,1) + C(8,2) + C(8,3) + C(8,4) + C(8,5)$$
 (e)  $C(20,5) - C(8,0)$ 

## 7 How many four letter words, including nonsense words, can you make using the letters of the word

## HOLIDAY

if each word must end with a vowel and letters cannot be repeated. (Note: Y is not a vowel)

(a) C(7,4) (b) P(7,4) (c)  $5 \cdot 6 \cdot 7 \cdot 3$  (d)  $4 \cdot 5 \cdot 6 \cdot 3$  (e)  $2 \cdot 3 \cdot 4 \cdot 3$ 

8 A deck of cards consists of 52 playing cards, with four suits, diamonds, hearts, clubs and spades. Each suit has 13 cards in it. How many poker hands consist of four hearts and a card of a different suit?

(a)  $48 \cdot C(13, 4)$  (b)  $39 \cdot C(52, 4)$  (c)  $48 \cdot C(52, 4)$ (d)  $39 \cdot C(13, 4)$  (e) C(13, 4)C(13, 1) **9** Determine the coefficient of  $x^4y^7$  in the binomial expansion of  $(x+y)^{11}$ .

(a) C(11,4) (b) 1 (c) P(11,4) (d) 4 (e) C(11,4)C(11,7)

10 An experiment consists of tossing six coins and counting the number of heads. The sample space for this experiment is  $\{0, 1, 2, 3, 4, 5, 6\}$ . If *E* is the event that there are more heads than tails, which of the following sets corresponds to *E*?

 $(a) \{1, 2, 3, 4, 5, 6\} (b) \{4, 5, 6\} (c) \{1, 2, 3\}$   $(d) \{3, 4, 5, 6\} (e) \{0, 2, 4, 6\}$ 

**11** If E and F are events in a sample space with probabilities

$$P(E) = .5, \qquad P(F) = .3.$$

If we know that E and F are independent events, What is  $P(E \cup F)$ ?

$$(a) -0.2$$
  $(b) 0.2$   $(c) 0.8$   $(d) 0.15$   $(e) 0.65$ 

12 If you roll a pair of fair dice, one red and one green, what is the probability that the sum of the two numbers on the uppermost faces is 7?

(a) 
$$\frac{7}{36}$$
 (b)  $\frac{1}{36}$  (c)  $\frac{1}{6}$  (d)  $\frac{5}{36}$  (e) 0

**13** An urn contains 5 pink and 6 blue marbles. A sample of 4 marbles is drawn from the urn. What is the probability that the sample has exactly 2 pink marbles?

(a) 
$$\frac{C(5, 2)}{C(11, 4)}$$
 (b)  $\frac{1}{C(11, 4)}$  (c)  $\frac{C(5, 2)C(6, 2)}{C(11, 4)}$  (d)  $\frac{2}{11}$  (e)  $\frac{1}{2}$ 

14 The rules of a carnival game are as follows:

You pay \$1 to play

You then flip a coin until you get a head or have flipped the coin three times.

If you get a head, you win and the carnival attendant gives you \$2. If you don't get a head, you lose, the carnival attendant gives you nothing.

What is the probability that you win the game? (A tree diagram might help)

(a)  $\frac{1}{2}$  (b)  $\frac{1}{8}$  (c)  $\frac{1}{4}$  (d)  $\frac{7}{8}$  (e)  $\frac{3}{4}$ 

15 The Everlasting Lightbulb company produces lightbulbs, which are packaged in boxes of 20 for shipment. Tests have shown that 5% of the lightbulbs produced in Everlasting Lightbulb factory are defective. What is the probability that a box, ready for shipment, contains exactly 3 defective lightbulbs?

(a) 
$$1 - C(20,3)(.05)^3(.95)^{17}$$
 (b)  $(.95)^{20} + C(20,1)(.05)^1(.95)^{19} + C(20,2)(.05)^2(.95)^{18}$   
(c)  $1 - \left\{ (.95)^{20} + C(20,1)(.05)^1(.95)^{19} + C(20,2)(.05)^2(.95)^{18} \right\}$  (d)  $C(20,3)(.05)^3(.95)^{17}$ 

 $(e) \quad 1 - (.95)^{20}$ 

16 Samantha records her times for 10 crosscountry 5 mile races with the following results (given in minutes):

25.8, 25.5, 25.8, 25.4, 25.6, 25.9, 25.7, 25.6, 25.9, 25.7.

What is Samantha's average running time per race, for those 10 races.

 17 Find the population variance,  $\sigma^2 = Var(X)$ , of the random variable X, whose distribution is given in the table below.

		Outcome 0 1 2 3 4	Probability .1 .2 .4 .2 1		
( <i>a</i> ) 1	( <i>b</i> ) 1.2	4	) 8	$(d) \ 0$	(e) .5

18 The number of cups of Starbucks coffee consumed by Netty the Caffiene addict each week is normally distributed with mean  $\mu = 15$  and standard deviation  $\sigma = 2$ . Each cup of coffee costs \$1.50. What is the probability that Netty spends \$30 or more on coffee this week.

(a).	.0287 ()	b) .0115 (	c)	.9938 (	[d]	.9713	(e	).0062
------	----------	------------	----	---------	-----	-------	----	--------

**19** If Z is a standard normal random variable, with mean  $\mu = 0$  and standard deviation  $\sigma = 1$ , what is  $Pr(-1.5 \le Z \le 2)?$ 

**20** Consider the matrices

$$A = \begin{pmatrix} -1 & 1 & 0 \\ 2 & 0 & 0 \end{pmatrix} \quad \text{and} \quad B = \begin{pmatrix} 2 & -1 \\ 0 & 1 \\ 1 & 3 \end{pmatrix}.$$

Which of the following gives the product of the two matrices,  $A \cdot B$ ?.

$$(a) \quad \begin{pmatrix} -4 & 2 & 0 \\ 2 & 0 & 0 \\ 5 & 1 & 0 \end{pmatrix} \qquad (b) \quad \begin{pmatrix} -2 & 0 & 0 \\ 4 & -1 & 1 \\ 0 & 1 & 5 \end{pmatrix} \qquad (c) \quad \begin{pmatrix} 0 & 5 \\ 5 & 1 \end{pmatrix} \qquad (d) \quad \begin{pmatrix} -2 & 2 \\ 4 & -2 \end{pmatrix}$$

(e) It is not possible to form the product of these two matrices.

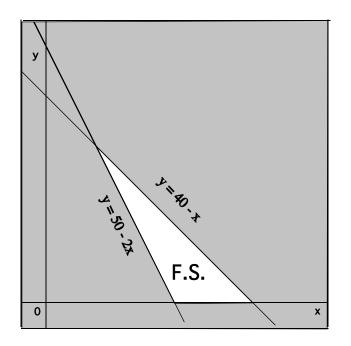
21 Find the inverse of the following matrix:

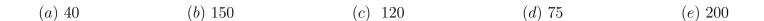
$$A = \begin{pmatrix} -1 & 1 \\ 2 & 0 \end{pmatrix}$$

$$(a) \quad \begin{pmatrix} 0 & -1 \\ -2 & -1 \end{pmatrix} \qquad (b) \quad \begin{pmatrix} 0 & -1/2 \\ -1 & -1/2 \end{pmatrix} \qquad (c) \quad \begin{pmatrix} 0 & 1/2 \\ 1 & 1/2 \end{pmatrix} \qquad (d) \quad \begin{pmatrix} 0 & 1/2 \\ 1 & -1/2 \end{pmatrix} \qquad (e) \qquad \begin{pmatrix} 0 & -1 \\ -2 & 1 \end{pmatrix}$$

22 Sunbucks coffee shop sells two types of caffeinated coffee blends: traditional dark roast and mild breakfast blend. Each pound of traditional dark roast contains 80% Jamaican bean and 20% Alaskan bean, and earns a profit of \$6 per pound. Each pound of mild breakfast blend contains 35% Jamaican bean and 65% Alaskan bean, and earns a profit of \$5 a pound. Sunbucks has 3000 pounds of Jamaican bean and 2500 pounds of Alaskan bean. If x is the number of pounds of the traditional dark roast produced and y is the number of pounds of the mild breakfast blend produced, then the inequalities that must be saitisfied for Sunrbucks to maximize its profit are :

(a) $\begin{array}{l} .80x + .20y \leq 3000\\ .35x + .65y \leq 2500\\ x \geq 0, y \geq 0\\ \text{profit: } 6x + 5y \end{array}$	(b) $\begin{array}{l} .80x + .35y \leq 3000\\ .65x + .20y \leq 2500\\ x \geq 0, y \geq 0\\ \text{profit: } 5x + 6y \end{array}$	(c) $\begin{array}{l} .80x + .20y \ge 3000\\ .35x + .65y \ge 2500\\ x \ge 0, y \ge 0\\ \text{profit: } 6x + 5y \end{array}$
(d) $35x + .80y \ge 3000$ $(5x + .20y \ge 2500$ $x \ge 0, y \ge 0$ profit: $5x + 6y$	$.80x + .35y \le 3000$	0





24 Consider the points

$$D: x = 30, \quad y = 15 E: x = 25, \quad y = 20. F: x = 35, \quad y = 2$$

Using the feasible set given in Question 23, Which of the following statements are true?

- (a) F is in the feasible set
- (b) E and F are in the feasible set
- (c) D and E are in the feasible set
- (d) E is in the feasible set
- (e) D and F are in the feasible set

**25** Roadrunner (R) and Coyote (C) play a zero-sum game, with the pay-off matrix for Roadrunner, R, given by :

	$C_1$	$C_2$	
$R_1$	1	3	
$R_2$	5	2	

In order to solve for his optimal mixed strategy, which of the Linear Programming problems given below must Roadrunner solve?

	$\begin{array}{l} \text{maximize } x + y \\ \text{subject to} \end{array}$	$\begin{array}{c} \text{minimize } x + y \\ \text{subject to} \end{array}$	$\begin{array}{ll}\text{minimize} & x+y\\ \text{subject to} \end{array}$
(a)	constraints $x \ge 0,  y \ge 0$ $x + 5y \le 1$ $3x + 2y \le 1$	(b) constraints $x \ge 0, y \ge 0$ $x + 3y \le 1$ $5x + 2y \le 1$ (c)	constraints $x \ge 0, y \ge 0$ $x + 3y \ge 1$ $5x + 2y \ge 1$
(d)	maximize $x + y$ subject to constraints $x \ge 0, y \ge 0$ $2x + y \ge 1$ $x + 3y \ge 1$	(e) $ \begin{array}{l} \text{minimize}  x+y \\ \text{subject to} \\ \text{constraints} \\ x \ge 0,  y \ge 0 \\ x+5y \ge 1 \\ 3x+2y \ge 1 \end{array} $	

**26** Rachmaninof (R) and Chaicovsky (C) play zero-sum game, where Rachmaninof's pay-off matrix is given by:

	$C_1$	$C_2$	$C_3$	$C_4$	$C_5$
$R_1$	2	1	-1	3	-2
$R_2$	4	2	-2	0	5
$R_3$	3	4	1	-3	-1
$R_4$	0	2	1	3	2
$R_5$	3	2	-1 -2 1 1 1 1	4	-1

What is Rachmaninof's optimal pure (fixed) strategy for this game?

 $(a) \operatorname{Row} 1 \qquad (b) \operatorname{Row} 2 \qquad (c) \operatorname{Row} 3 \qquad (d) \operatorname{Row} 4 \qquad (e) \operatorname{Row} 5$ 

27 Rebecca and Consuela play a zero sum game, where the pay off matrix for Rebecca is given by:

	$C_1$	$C_2$	$C_3$
$R_1$	4	2	-2
$R_2$	3	4	1
$R_3$	2	1	-1

If the payoff matrix has a saddle point where is it?

 $4 \ 2 \ 3 \ 4 \ 4$ 

(a) Row 3, Col 3 (b) Row 1, Col 3 (c) Row 2, Col 3 (d) Row 3, Col 1 (e) Row 2, Col 2

**28** Rudolph (R) and Comet (C) play a game. They both choose a number between 1 and 4 simultaneously. Comet gives Rudolph a number of carrots equal to the sum of the two numbers chosen minus three. If this number is negative, Comet recieves carrots from Rudolph. Which of the following give the pay-off matrix for Rudolph?

<i>(a)</i>	R	No. 1 2 3 4	$     \begin{array}{ c c c }             1 \\             -1 \\           $	$\begin{array}{c} C\\ 2\\ \hline 0\\ 1\\ 2\\ 3\\ \end{array}$	$\begin{array}{c}3\\1\\2\\3\\4\end{array}$	$\begin{array}{r} 4\\ \hline 2\\ 3\\ 4\\ 5 \end{array}$	(	b)	R	No. 1 2 3 4	$     \begin{array}{c}       1 \\       3 \\       2 \\       1 \\       2     \end{array} $	$\begin{array}{c} C\\ 2\\ 1\\ 2\\ 3\\ \end{array}$	$\begin{array}{c}3\\1\\2\\3\\4\end{array}$	$\begin{array}{c} 4\\ 2\\ 3\\ 4\\ 5\end{array}$	(c)	R	<i>No.</i> 1 2 3 4		$\begin{array}{c} C\\ 2\\ \hline 3\\ 0\\ 1\\ 0\\ \end{array}$	$3 \\ -1 \\ 2 \\ 1$	$\begin{array}{r} 4\\ 5\\ -2\\ 3\\ 2\end{array}$
	(	d)	R	<i>No.</i> 1 2 3	$\begin{array}{c}1\\-1\\0\\1\end{array}$	$egin{array}{c} C \\ 2 \\ \hline 0 \\ 0 \\ 2 \end{array}$	$\frac{3}{2}$ $3$	$\begin{array}{c} 4\\ 2\\ 0\\ 3 \end{array}$				(e)		 	<i>No.</i> 1 2 3	$\begin{array}{c}1\\3\\4\\5\end{array}$	$\begin{array}{c} C\\ 2\\ 4\\ 5\\ 6\end{array}$	$\frac{3}{5}\\6\\7$	$\frac{4}{6}$ 78		

4 6 7 8 9

**29** Rasputin (R) and Catherine (C) play a zero-sum game with payoff matrix for Rasputin given below. If Rasputin's strategy is given by  $\begin{pmatrix} .2 \\ .1 \\ .7 \end{pmatrix}$ , what is the expected pay-off for Rasputin?

(a) -0.1 (b) 1 (c) 1.54 (d) -0.3 (e) 0.21

**30** Cop (C) and Robber (R) play a zero-sum game, with payoff matrix for Robber given by

$$\begin{array}{c|ccc} & C_1 & C_2 \\ \hline R_1 & 2 & 1 \\ R_2 & 1 & 3 \end{array}$$

If the solution to the linear programming problem:

$$\begin{array}{lll} \text{minimize} & x+y\\ \text{constraints} & x \ge 0, & y \ge 0\\ & 2x+y & \ge 1\\ & x+3y & \ge 1 \end{array}$$

is given by  $x = \frac{2}{5}$ ,  $y = \frac{1}{5}$ , which of the following give the optimal strategy and  $\nu =$  expected payoff for Robber?

- (a)  $\begin{pmatrix} \frac{1}{3} & \frac{2}{3} \end{pmatrix}$ ,  $\nu = \frac{5}{3}$  (b)  $\begin{pmatrix} \frac{6}{25}, \frac{3}{25} \end{pmatrix}$ ,  $\nu = \frac{3}{5}$  (c)  $\begin{pmatrix} \frac{2}{3}, \frac{1}{3} \end{pmatrix}$ ,  $\nu = \frac{3}{5}$
- (d)  $\left(\frac{2}{5}, \frac{1}{5}\right)$ ,  $\nu = \frac{3}{5}$  (e)  $\left(\frac{2}{3}, \frac{1}{3}\right)$ ,  $\nu = \frac{5}{3}$